

43.11 An air handling fan delivers 9000cfm against a total pressure of 3in wg at standard conditions. A new unit is designed to provide the same volume flow using a fan with a 25% larger diameter which runs at half the speed. What is the air horsepower produced by the new air handler?

- A. 1hp
- B. 2hp
- C. 4hp
- D. 5hp

Make a table to organize the original and new conditions, and use subscripts 1 and 2, respectively. Take into account the given information regarding the new diameter increasing by 25% and the new speed reducing by half.

	Original (1)	New (2)
Q	9000cfm	9000cfm
P	3in wg	P_2
D	D_1	$D_2 = 1.25D_1$
N	N_1	$N_2 = \frac{N_1}{2}$
W	W_1	W_2

Look up **Fan Power** in the reference handbook and use the formula to determine the air horsepower for the original state, W_1 . This book will typically use AHP ; however, the handbook uses P_s or P_e , and the **Fan Laws** table uses W for power. In this problem we will freely interchange between all of these parameters with the understanding that all refer to *air horsepower*.

$$AHP_1 = W_1 = \frac{Q_1 \Delta P_1}{6356} = \frac{(9000)(3)}{6356} = 4.25\text{hp}$$

Note there is no reference to efficiency so assume $\eta = 1$ and may be ignored. Select from the **Fan Affinity Laws** equation #1c:

$$W_1 = W_2 \times \left(\frac{D_1}{D_2}\right)^5 \left(\frac{N_1}{N_2}\right)^3 \left(\frac{\rho_1}{\rho_2}\right)$$

The density of the air under the new conditions may be assumed to be unchanged. Therefore assume $\rho_1 = \rho_2$. Swap the subscripts for convenience. Simplify and solve for the new power, W_2 . Note the diameters and speeds need not be known. Instead the ratio of new to old may be used.

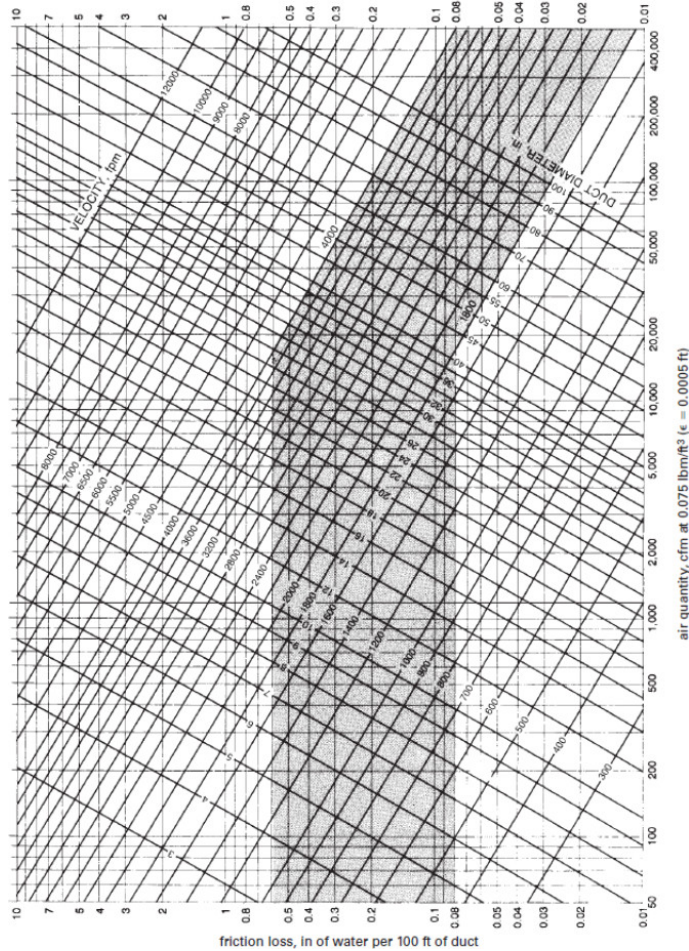
$$W_2 = W_1 \times \left(\frac{D_2}{D_1}\right)^5 \left(\frac{N_2}{N_1}\right)^3$$

$$W_2 = (4.25\text{hp})(1.25)^5 (.5)^3 = 1.62\text{hp}$$

There are alternative solutions to this problem using a different fan affinity law. The laws are internally consistent so if time permits, you may want to check your answer by taking a different avenue.

Answer B

43.12 A 600ft long round duct with a diameter of 12in delivers 1000cfm. There are (12) 90-degree elbows with a bend radius of double the duct diameter, contributing an equivalent length of 10 times the duct diameter for each fitting. What is the friction loss?



- A. 0.8in wg
- B. 1.4in wg
- C. 2.0in wg
- D. 2.8in wg

Use the friction loss chart provided to determine the ΔP based on the volume flow rate and duct diameter given:

$$Q = 1000cfm$$