

$$h_f = 196 \frac{\text{Btu}}{\text{lb}}$$

$$h_{fg} = 960 \frac{\text{Btu}}{\text{lb}}$$

$$h_2 = h_f + \chi_2 h_{fg} = 196 \frac{\text{Btu}}{\text{lb}} + (0.95) \left(960 \frac{\text{Btu}}{\text{lb}} \right) = 1108 \frac{\text{Btu}}{\text{lb}}$$

Rearrange the equation for the steam energy for the unknown mass flow rate, substitute, solve, and change units to $\frac{\text{lb}}{\text{min}}$:

$$q_s = \dot{m} (h_1 - h_2) \rightarrow \dot{m} = \frac{q_{\text{steam}}}{(h_1 - h_2)}$$

$$\dot{m} = \frac{325,000 \frac{\text{Btu}}{\text{hr}}}{\left(1215 \frac{\text{Btu}}{\text{lb}} - 1108 \frac{\text{Btu}}{\text{lb}} \right)} = 3037 \frac{\text{lb}}{\text{hr}} \left(\frac{1 \text{hr}}{60 \text{min}} \right) = 50.6 \frac{\text{lb}}{\text{min}}$$

Answer B

42.4 A skylight is comprised of two layers of $\frac{1}{2}$ inch thick laminated glass with a 1in air gap $\left(R = 0.5 \frac{\text{hr} \cdot \text{ft}^2 \cdot ^\circ\text{F}}{\text{Btu}} \right)$ in between. The inside and outside film coefficients are $1.5 \frac{\text{Btu}}{\text{hr} \cdot \text{ft}^2 \cdot ^\circ\text{F}}$ and $2.0 \frac{\text{Btu}}{\text{hr} \cdot \text{ft}^2 \cdot ^\circ\text{F}}$, respectively. The outside design temperature is 10°F and the inside conditions are 70°F with 60% relative humidity. What is the maximum allowable thermal conductivity of the glass to prevent condensate from forming on the inside of the skylight?

- A. $0.04 \frac{\text{Btu}}{\text{hr} \cdot \text{ft} \cdot ^\circ\text{F}}$
- B. $0.08 \frac{\text{Btu}}{\text{hr} \cdot \text{ft} \cdot ^\circ\text{F}}$
- C. $0.2 \frac{\text{Btu}}{\text{hr} \cdot \text{ft} \cdot ^\circ\text{F}}$
- D. $0.9 \frac{\text{Btu}}{\text{hr} \cdot \text{ft} \cdot ^\circ\text{F}}$

The inside conditions are known. Determine the **dew point** temperature using the **psychrometric chart**. This is the minimum temperature on the inside surface of the glass before which condensate will form.

$$T_{i,db} = 70^\circ\text{F}$$

$$\phi_i = 60\%$$

$$T_{i,dp} = 55.6^\circ\text{F}$$

Let T_i be the inside temperature.

Let A denote the inner surface of the skylight.

Let B denote the interface between the inner glass and the air gap.

Let C denote the interface between the outer glass and the air gap.

Let D denote the outer surface of the skylight.

Let T_o be the outside temperature.

Review the Reference Handbook section on **Conduction**. Treat the skylight as a **Composite Plane Wall**, where the total resistance, R_{total} , can be expressed for this particular situation as:

$$R_{total} = \frac{1}{h_i} + \frac{L}{k} + R + \frac{L}{k} + \frac{1}{h_o}$$

where h_i and h_o are the inside and outside film coefficients, respectively, the $\frac{L}{k}$ terms correspond to conduction through the thickness L of the both sheets of glass having thermal conductivity k , and R represents the resistance of the air gap, which is given. Substitute and simplify to derive an expression for the total resistance, R_{total} , as a function of thermal conductivity, k . Make sure units for each term are in alignment.

$$R_{total} = \frac{1}{1.5 \frac{Btu}{hr \cdot ft^2 \cdot ^\circ F}} + \frac{(\frac{1}{2} in) \left(\frac{1ft}{12in} \right)}{k} + 0.5 \frac{hr \cdot ft^2 \cdot ^\circ F}{Btu} + \frac{(\frac{1}{2} in) \left(\frac{1ft}{12in} \right)}{k} + \frac{1}{2.0 \frac{Btu}{hr \cdot ft^2 \cdot ^\circ F}}$$

$$R_{total} = 1.67 \frac{hr \cdot ft^2 \cdot ^\circ F}{Btu} + \frac{1ft}{12(k)}$$

The inside temperature will be minimized when the heat loss through the skylight is maximized, i.e. when the heat flux through the “composite wall” is large. Consider the **convection** between the inside ambient space at temperature T_i , and the inside of the skylight at surface A. The heat transfer by convection is given by:

$$\dot{Q} = h_i A \Delta T$$

Since the area is unknown, divide by area and work with the heat transfer *per unit area*, or heat flux:

$$\dot{q} = h_i \Delta T$$

$$\dot{q}_{max} = \left(1.5 \frac{Btu}{hr \cdot ft^2 \cdot ^\circ F} \right) (70^\circ F - 55.6^\circ F) = 21.6 \frac{Btu}{hr \cdot ft^2}$$

Considering the entire wall again, find the overall heat transfer coefficient, $U_{overall}$, inclusive of all layers and resistances by assuming the maximum heat flux through the resistance of all layers. The heat flow through the wall can be represented as:

$$\dot{Q} = U A \Delta T$$

Again, we need not be concerned with the area. Divide by area and work with the heat flux:

$$\dot{q} = U \Delta T$$