

42.10 An exterior wall is made up of 4 inch brick cladding $\left(k = 0.42 \frac{\text{Btu} \cdot \text{ft}}{\text{hr} \cdot \text{ft}^2 \cdot ^\circ\text{F}}\right)$, $3\frac{1}{2}$ in mineral fiber batt insulation $\left(C = 0.077 \frac{\text{Btu}}{\text{hr} \cdot \text{ft}^2 \cdot ^\circ\text{F}}\right)$, and $\frac{5}{8}$ inch gypsum board $\left(C = 1.78 \frac{\text{Btu}}{\text{hr} \cdot \text{ft}^2 \cdot ^\circ\text{F}}\right)$. The external surface of the brick is 0°F and the inside surface of the gypsum board is maintained at 70°F . What is the temperature at the interface between the brick and the insulation?

- A. 4°F
- B. 6°F
- C. 9°F
- D. 13°F

Treat the problem as a **composite wall** with conduction through three layers: brick, insulation, and gypsum board. It is often necessary to look up the **Thermal Resistance of Building Materials** in the Reference Handbook, however, in this case the **thermal conductivity** and **conductance** values were given.

Find the total thermal resistance through the composite wall. Use the thermal conductivity and thickness for the brick as given. For the insulation and gypsum board, the conductance has been given, which already accounts for the thickness.

$$R_T = \frac{L}{k_{\text{brick}}} + \frac{1}{C_{\text{insulation}}} + \frac{1}{C_{\text{gypsum}}}$$

$$R_T = \frac{(4\text{in}) \left(\frac{1\text{ft}}{12\text{in}}\right)}{0.42 \frac{\text{Btu} \cdot \text{ft}}{\text{hr} \cdot \text{ft}^2 \cdot ^\circ\text{F}}} + \frac{1}{0.077 \frac{\text{Btu}}{\text{hr} \cdot \text{ft}^2 \cdot ^\circ\text{F}}} + \frac{1}{1.78 \frac{\text{Btu}}{\text{hr} \cdot \text{ft}^2 \cdot ^\circ\text{F}}} = 14.3 \frac{\text{hr} \cdot \text{ft}^2 \cdot ^\circ\text{F}}{\text{Btu}}$$

Determine the **overall coefficient of heat transfer** for the composite wall:

$$U = \frac{1}{R_T} = \frac{1}{14.3 \frac{\text{hr} \cdot \text{ft}^2 \cdot ^\circ\text{F}}{\text{Btu}}} \approx 0.07 \frac{\text{Btu}}{\text{hr} \cdot \text{ft}^2 \cdot ^\circ\text{F}}$$

Find the heat flux i.e. heat transfer per unit area through the entire wall based on the overall coefficient of heat transfer. Use the temperatures for the internal and external surfaces.

$$\dot{Q} = UA\Delta T$$

$$\dot{q} = \frac{\dot{Q}}{A} = U\Delta T = \left(0.07 \frac{\text{Btu}}{\text{hr} \cdot \text{ft}^2 \cdot ^\circ\text{F}}\right) (70^\circ\text{F} - 0^\circ\text{F}) = 4.88 \frac{\text{Btu}}{\text{hr} \cdot \text{ft}^2}$$

To find the temperature at the interface of the brick and the insulation, consider only the thermal resistance of the brick, and the external temperature, treating the temperature at the brick/insulation interface as unknown. Note the heat flux is the same through the entire composite wall.

$$R_{brick} = \frac{(4ft) \left(\frac{12in}{1ft} \right)}{0.42 \frac{Btu \cdot ft}{hr \cdot ft^2 \cdot ^\circ F}} = .794 \frac{hr \cdot ft^2 \cdot ^\circ F}{Btu}$$

$$U_{brick} = \frac{1}{R_{brick}} = \frac{1}{.794 \frac{hr \cdot ft^2 \cdot ^\circ F}{Btu}} = 1.26 \frac{Btu}{hr \cdot ft^2 \cdot ^\circ F}$$

$$\dot{q} = U \Delta T \rightarrow \Delta T = \frac{\dot{q}}{U_{brick}} = \frac{4.88 \frac{Btu}{hr \cdot ft^2}}{1.26 \frac{Btu}{hr \cdot ft^2 \cdot ^\circ F}} = 3.87^\circ F$$

$$\Delta T = T_2 - T_1 = T_2 - 0^\circ F = 3.87^\circ F$$

$$T_2 = 3.87^\circ F \approx 4^\circ F$$

Answer A

42.11 100lbs of Haddock initially at 45°F is to be frozen to 20°F within 3hrs. What is the minimum required refrigeration capacity?

- A. 0.2tons
- B. 0.4tons
- C. 1ton
- D. 2tons

Calculate the total heat to be removed from the **Haddock** by finding the sum of sensible cooling *above* the freezing point, latent cooling, and sensible cooling *below* the freezing point. Note the freezing point of the fish, like many foods, is not exactly the same as the freezing point of water. In this case it is 28°F. Use the table **Properties of Foods** to look up the **specific heat capacity** and **freezing point**.

$$Q_{total} = Q_{sensible,above FP} + Q_{latent @FP} + Q_{sensible,below FP}$$

$$Q_{sensible,above FP} = mc_{p,above} \Delta T$$

$$Q_{sensible,above FP} = (100lb) \left(.9 \frac{Btu}{lb^\circ F} \right) (45^\circ F - 28^\circ F) = 1530Btu$$

$$Q_{latent @FP} = mh_{fg} = (100lb) \left(115 \frac{Btu}{lb} \right) = 11,500Btu$$

$$Q_{sensible,below FP} = mc_{p,below} \Delta T$$

$$Q_{sensible,below FP} = (100lb) \left(.51 \frac{Btu}{lb^\circ F} \right) (28^\circ F - 20^\circ F) = 408Btu$$