

46.5 A group of machines are maintained under a contract which costs \$50,000 this year. The contract cost will increase by \$1000 per year over the next 10 years. What is the present value of the entire 10 years of maintenance using an effective annual interest rate of 12%.

- A. \$303,000
- B. \$336,000
- C. \$352,000
- D. \$370,000

The present value can be represented as the sum of two cash flows: a recurring annual cost of \$50,000 and a uniform gradient of \$1,000. The gradient has a value of zero in the first year, such that the first year cost is \$50,000, second year is \$51,000, third year is \$52,000, etc. There is no initial cost reflected in year 0 as it is customary in engineering economics to reflect costs that occur throughout the year at the end of the year.

Write an expression for the present value.

$$PV = A(P/A, 12\%, 10) + G(P/G, 12\%, 10)$$

Use the 12% Factor Table to look up the cash flow factors needed to translate the cash flows into present value. Solve for the present value.

$$PV = (\$50,000)(5.6502) + (\$1,000)(20.2541) = \$302,764$$

Answer A

46.6 A pump delivers 200 GPM of water at 130 feet of total dynamic head, operating from 7am-7pm Monday through Friday. The pump is 80% efficient and the motor is 93% efficient. What is the annual cost of operation at \$0.13 per kWh?

- A. \$2670
- B. \$3490
- C. \$3750
- D. \$5030

The cost is a function of electrical power and time, and electrical power is a function of hydraulic horsepower (aka water horsepower i.e. **whp**) and efficiency. Start by calculating the water horsepower based on volume flow rate and feet of head provided by the pump:

$$whp = \frac{Q\Delta h}{3960} = \frac{(200)(130)}{3960} = 6.566hp$$

Note the volume and head units must be in *GPM* and *ft*, respectively, to use this “rule of thumb” equation. Therefore units need not be shown, provided they are confirmed to be correct prior to use.

Recall that brake horsepower, *bhp*, depends on water horsepower, *whp*, and the efficiency of the pump, η_p . Similarly, the electrical power, \dot{W} , depends on brake horsepower, *bhp*, and motor efficiency, η_m .

$$bhp = \frac{whp}{\eta_p}$$

$$\dot{W} = \frac{bhp}{\eta_m}$$

Put these together, substitute, solve, and convert to *KW*:

$$\dot{W} = \frac{whp}{\eta_p \eta_m} = \frac{6.566hp}{(.8)(.93)} \left(\frac{.746KW}{1hp} \right) = 6.58KW$$

To find the annual cost, multiply by time and the unit rate of electricity:

$$Cost = (6.58KW) \left(\frac{12hrs}{day} \right) \left(\frac{5days}{wk} \right) \left(\frac{52wks}{yr} \right) \left(\frac{\$0.13}{KWH} \right) = \$2669 \text{ per year}$$

Answer A

46.7 A *7.5hp single phase 230V motor drawing 40A at full load is located 50 meters from the voltage source. The motor is wired with 8AWG wire which has a cross sectional area of 16,509 circular mils (1 circular mil = $5.066 \times 10^{-10}m^2$) and a resistivity of $1.724 \times 10^{-8}\Omega \cdot m$. What is the percent voltage drop for the wiring in the circuit?*

- A. 1%
- B. 2%
- C. 3%
- D. 4%

The electrical resistance attributable to the wiring is the result of copper’s **resistivity**, which is an intrinsic material property, and the length and gauge of the wire. The formula for resistivity can be rearranged to solve for the total resistance.

$$\rho = \frac{RA}{L}$$

$$R = \frac{\rho L}{A}$$

Since the motor is *50ft* from the voltage source, a sufficient length of wire must be provided to make a round trip from the source to the load and back. Therefore, the total length is given by: