

46.79 25gpm of water at 300psia and 250°F goes through a boiler where it is converted to 500psia steam at 1000°F. What is the heat load being delivered by the boiler?

- A. 360boiler hp
- B. 420boiler hp
- C. 460boiler hp
- D. 490boiler hp

Consider the water entering the boiler as a State 1 and the superheated steam exiting the boiler as State 2. Determine the enthalpy at State 1. Use the properties of **Saturated Water and Steam** table by pressure and obtain h_f at $P_1 = 300\text{psia}$. Since $T_1 < T_{sat}$, the water is subcooled. Solve for the enthalpy at T_1 .

$$T_{sat@300\text{psia}} = 417.33^\circ F$$

$$h_{sat} = h_{f@300\text{psia}} = 393.93 \frac{\text{Btu}}{\text{lb}}$$

$$h_{sat} - h_1 = c_p (T_{sat} - T_1)$$

$$h_1 = h_{sat} - c_p (T_{sat} - T_1) = 393.93 \frac{\text{Btu}}{\text{lb}} - \left(1 \frac{\text{Btu}}{\text{lb}^\circ F} \right) (417.33^\circ F - 250^\circ F) = 226.6 \frac{\text{Btu}}{\text{lb}}$$

Approximate the density at State 1 using the **Properties of Water** table and extrapolating to 250°F. The pressure is much higher than atmospheric pressure, but this approach yields a fairly accurate result since water incompressible.

$T [^\circ F]$	$\rho \left[\frac{\text{lb}}{\text{ft}^3} \right]$
200	60.1
212	59.83
250	ρ

$$\frac{212^\circ F - 200^\circ F}{250^\circ F - 200^\circ F} = \frac{59.83 \frac{\text{lb}}{\text{ft}^3} - 60.1 \frac{\text{lb}}{\text{ft}^3}}{\rho - 60.1 \frac{\text{lb}}{\text{ft}^3}}$$

$$0.24 = \frac{-0.27 \frac{\text{lb}}{\text{ft}^3}}{\rho - 60.1 \frac{\text{lb}}{\text{ft}^3}}$$

$$\rho - 60.1 \frac{\text{lb}}{\text{ft}^3} = -1.125 \frac{\text{lb}}{\text{ft}^3}$$

$$\rho = 58.98 \frac{\text{lb}}{\text{ft}^3}$$

The density value obtained from compressed water tables not available in the Reference Handbook is $58.8 \frac{lb}{ft^3}$ for a deviation of only 0.3%.

Find the heat load for the boiler. Replace mass flow rate with the product of density and volume flow rate. Convert units to $\frac{Btu}{hr}$, then finally to *boiler hp*.

$$\dot{Q} = \dot{m}\Delta h = \rho Q\Delta h$$

$$\dot{Q} = \left(58.98 \frac{lb}{ft^3}\right) \left(25 \frac{gal}{min}\right) \left(\frac{1ft^3}{7.48gal}\right) \left(\frac{60min}{1hr}\right) \left(1521 \frac{Btu}{lb} - 226.6 \frac{Btu}{lb}\right) = 1.53 \times 10^7 \frac{Btu}{hr}$$

$$\dot{Q} = \frac{1.53 \times 10^7 \frac{Btu}{hr}}{33,470 \frac{Btu}{hr \cdot boiler\ hp}} = 457 \text{boiler hp}$$

Answer C

46.80 $1 \frac{lb_m}{s}$ of saturated liquid water at $50psia$ enters a mixing chamber along with $1 \frac{lb_m}{s}$ of superheated steam at $50psia$ and $500^\circ F$. $2 \frac{lb_m}{s}$ of the resulting mixture is discharged after thorough mixing. What is the quality of the mixture?

- A. 0.44
- B. 0.50
- C. 0.56
- D. 0.62

Sketch the mixing chamber. Let State 1 represent the entering saturated liquid, State 2 represent the entering saturated steam, and State 3 represent the exiting mixture. Write the energy balance for the mixing process.

$$\dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_3 h_3$$

All mass flow rates are known. Use the [Properties of Saturated Water and Steam](#) (Pressure) table to obtain the enthalpy at State 1, h_1 .

$$P_1 = 50psia$$

$$h_1 = h_f = 250.2 \frac{Btu}{lb}$$

Use the [Properties of Superheated Steam](#) table to obtain the enthalpy at State 2.

$$P_2 = 50psia$$

$$T_2 = 500^\circ F$$