

$$w = \frac{R(T_2 - T_1)}{1 - k} = \frac{\left(53.35 \frac{ft \cdot lb_f}{lb_m \cdot R}\right) [470^\circ F - 77^\circ F]}{1 - 1.4} = \frac{-52,416 \frac{ft \cdot lb_f}{lb_m}}{778 \frac{ft \cdot lb_f}{Btu}} = -67 \frac{Btu}{lb_m}$$

Normally it would be required to change Fahrenheit to Rankine; however, since it is a temperature *difference*, the delta is unchanged.

Note the unit conversion from $ft \cdot lb_f$ to Btu .

Finally, note the negative sign of the answer which aligns with the question's implication that work is being done *to the system*. A positive value would be expected if work were being done *by the system*.

Answer B

39.10 What quantity of heat is released per unit mass when copper is cooled from $250^\circ F$ to $75^\circ F$?

- A. $16 \frac{Btu}{lb}$
- B. $18 \frac{Btu}{lb}$
- C. $57 \frac{Btu}{lb}$
- D. $157 \frac{Btu}{lb}$

For heat transfer by conduction, use:

$$Q = mc_p \Delta T$$

Divide by mass to specify heat transfer per unit mass:

$$q = c_p \Delta T$$

Look up the specific heat capacity of **copper** by searching the reference handbook for **properties of metals**.

Substitute and solve:

$$q = \left(.09 \frac{Btu}{lb^\circ F} \right) (250^\circ F - 75^\circ F) = 15.75 \frac{Btu}{lb}$$

Answer A

39.11 An outside air handling unit delivers 5000cfm of outside air. On a winter day, the outside air is 18°F and is heated to 68°F using a hot water coil. Hot water is supplied at 165°F and returned at 140°F. What is the required flow rate of hot water?

- A. 0.4gpm
- B. 3gpm
- C. 22gpm
- D. 173gpm

The air undergoes sensible heating. Use the sensible heating rule of thumb:

$$Q_s = 1.08CFM\Delta T_{air}$$

The heat given up by the water can be determined with the sensible heating/cooling rule of thumb for water:

$$Q_w = 500GPM\Delta T_{water}$$

The quantity of heat added to the air is supplied entirely by the hot water, therefore we can equate the two formulas:

$$1.08CFM\Delta T_{air} = 500GPM\Delta T_{water}$$

The GPM of the hot water is the only unknown. Isolate, substitute, and solve:

$$GPM = \frac{1.08CFM\Delta T_{air}}{500\Delta T_{water}} = \frac{1.08(5000)(68 - 18)}{500(165 - 140)} = 21.6GPM$$

Note that no units need to be included when using these “rules of thumb” provided *all input values are in the correct units in the first place* i.e. CFM, GPM, and Farenheit.

Answer C