

37.34 An object with a surface area of 10ft^2 and a surface temperature of 40°F gains $1000\frac{\text{Btu}}{\text{hr}}$ through a combination of radiation and convection. The ambient temperature as well as the temperature of the surrounding surfaces is 80°F . The emissivity is 0.8. What is the convection film coefficient?

- A. $1.7\frac{\text{Btu}}{\text{hr}\cdot\text{ft}^2\cdot^\circ\text{F}}$
- B. $3.1\frac{\text{Btu}}{\text{hr}\cdot\text{ft}^2\cdot^\circ\text{F}}$
- C. $3.8\frac{\text{Btu}}{\text{hr}\cdot\text{ft}^2\cdot^\circ\text{F}}$
- D. $5.6\frac{\text{Btu}}{\text{hr}\cdot\text{ft}^2\cdot^\circ\text{F}}$

Radiation and **Convection** are both applicable and together make up the total heat gain.

$$\dot{Q}_t = \dot{Q}_{conv} + \dot{Q}_{rad}$$

$$\dot{Q}_{conv} = hA\Delta T$$

$$\dot{Q}_{rad} = \sigma\varepsilon A (T_s^4 - T_\infty^4)$$

$$\dot{Q}_t = \dot{Q}_{conv} + \dot{Q}_{rad} = hA\Delta T + \sigma\varepsilon A (T_s^4 - T_\infty^4)$$

Calculate the heat transfer resulting from radiation. Be sure to use absolute temperatures i.e. degrees Rankine.

$$\dot{Q}_{rad} = \sigma\varepsilon A (T_s^4 - T_\infty^4)$$

$$\dot{Q}_{rad} = \left(0.1713 \times 10^{-8} \frac{\text{Btu}}{\text{hr}\cdot\text{ft}^2\cdot^\circ\text{R}}\right) (0.8) (10\text{ft}^2) \left[(540^\circ\text{R})^4 - (500^\circ\text{R})^4\right] = 308.8 \frac{\text{Btu}}{\text{hr}}$$

Subtract the radiation from the total heat gain to determine the heat gain from convection.

$$\dot{Q}_{conv} = \dot{Q}_t - \dot{Q}_{rad} = 1000 \frac{\text{Btu}}{\text{hr}} - 308.8 \frac{\text{Btu}}{\text{hr}} = 691.2 \frac{\text{Btu}}{\text{hr}}$$

Solve for the convection coefficient.

$$\dot{Q}_{conv} = hA\Delta T$$

$$h = \frac{\dot{Q}_{conv}}{A\Delta T} = \frac{(691.2 \frac{\text{Btu}}{\text{hr}})}{(10\text{ft}^2) (80^\circ\text{F} - 40^\circ\text{F})} = 1.7 \frac{\text{Btu}}{\text{hr}\cdot\text{ft}^2\cdot^\circ\text{F}}$$

Answer A