

31.20 A 2000ft^2 house has an average cooling demand of 3.5tons during a typical summer day. The inside temperature is maintained at 72°F and the average outside temperature is 93°F . Electricity costs $\$0.15/\text{kWh}$. Assuming the air conditioning system has the maximum possible theoretical efficiency, what is the daily cost of cooling?

- A. \\$2
- B. \\$5
- C. \\$9
- D. \\$12

The maximum possible theoretical efficiency for a cooling cycle is based on the reversed **Carnot Cycle**. For refrigeration, the **Coefficient of Performance** is determined entirely from the temperatures of the cold and hot reservoirs i.e. the indoor and outdoor conditions. Absolute temperatures must be used.

$$COP_c = \frac{T_L}{T_H - T_L} = \frac{72 + 460}{(93 + 460) - (72 + 460)} = 25.3$$

By definition, the **COP** is the ratio of the refrigeration effect to the input compressor energy required to produce the cooling. Calculate W_{in} and convert units to KW .

$$COP = \frac{Q_L}{W_{in}}$$

$$W_{in} = \frac{Q_L}{COP} = \frac{(3.5\text{tons}) (12,000 \frac{\text{Btu}}{\text{hr}\cdot\text{ton}})}{(3412 \frac{\text{Btu}}{\text{hr}\cdot\text{KW}}) (25.3)} = 0.48\text{KW}$$

Use the electricity rate to calculate the cost for run the cooling system continuously for 1 day.

$$Cost = (0.48\text{KW}) (24\text{hr}) \left(0.15 \frac{\$}{\text{KW}\cdot\text{hr}} \right) = \$1.75$$

Answer A